High Frequency Multiplicative Component GARCH**

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Abstract
This paper proposes a new way of modeling and forecasting intraday returns. We decompose the volatility of high frequency asset returns into components that may be easily interpreted and estimated. The conditional variance is expressed as a product of daily, diurnal and stochastic intraday volatility components. This model is applied to a comprehensive sample consisting of 10-minute returns on more than 2500 US equities. We apply a number of different specifications. Apart from building a new model, we obtain several interesting forecasting results. In particular, it turns out that forecasts obtained from the pooled cross section of companies seem to outperform the corresponding forecasts from company-by-company estimation.

JEL Classifications: C22, C51, C53, G15
Keywords: Volatility, ARCH, Intra-day Returns.

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1. INTRODUCTION

This paper proposes a new way of modeling and forecasting intraday returns. We decompose the volatility of high frequency asset returns into multiplicative components, which may be easily interpreted and estimated. The conditional variance is expressed as a product of daily, diurnal and stochastic intraday volatility components. This model is applied to a comprehensive sample consisting of 10-minute returns on more than 2500 US equities. We apply a number of different specifications. Namely we build models for separate companies, pool data into industries and consider various criteria for grouping returns. It turns out that results for the pooled regressions seem to be more stable. The forecasts from the pooled specifications outperform the corresponding forecasts from company-by-company estimation, and we discuss several issues regarding the best way to pool.

Conventional GARCH approaches were argued to be unsatisfactory for modeling intraday returns by authors at the Olsen conference on High Frequency Data Analysis in Zurich in March 1995. In response see Ghose and Kroner (1996). Alternatively, Andersen and Bollerslev (1997, 1998) propose models for 5-minute returns on Deutschemark-dollar exchange rate and the S&P500 index. In the first paper, Andersen and Bollerslev build a multiplicative model of daily and diurnal volatility, and in the second they add an additional component which takes account of macroeconomic announcements. We think that adding a collection of dummy variables representing macroeconomic news announcements to model volatility of US stocks is not very practical. Most important macroeconomic announcements happen before the stock market opens. Secondly, it is difficult to imagine that the strength and pattern of market’s response to news would be the same, even for the same type of events across time, disregarding the fact how much the news has been anticipated. Third, idiosyncratic announcements can be expected to be particularly important for equities, and the timing of the majority of them is very difficult to forecast. For most of Andersen and Bollerslev’s models, the intra-daily volatility components are deterministic. In contrast, the intra-daily components in our model are both deterministic (the diurnal) and stochastic (a separate intra-daily ARCH).

Overall, in distinction to the huge volume of literature on daily volatility models, the research on intraday volatility has been by far less studied. Taylor and Xu (1997) construct an hourly volatility model using an ARCH specification and supplementing the conditional vari-
ance equation by two additional elements: the implied volatility and the realized volatility computed from the high frequency data. Giot (2005) examines a number of market risk models for intraday data. A long memory stochastic volatility approach was applied by Deo, Hurvich and Lu (2005). Their paper diurnally adjusts in the frequency domain and then uses a local Whittle estimator on log of squared returns to estimate the parameters.

We expect our intraday model to be of particular interest for derivative traders or hedge funds who seek high frequency measures of risk or time varying hedge ratios. Volatility estimates on an intraday basis could be used to evaluate the risk of slow trading (Engle, 2005) or as input to measures of time varying liquidity. Most importantly, however, intraday volatility estimates are useful for devising optimal strategies to place limit orders or schedule trades. The literature on order choice supplies sufficient evidence that volatility is an important factor in order submission strategies (cf. Ellul et al. 2003, Griffith et al., 2000). These strategies are implemented on intraday basis. Ranaldo (2004) documents that high volatility increases the probability of submission of limit orders, whereas Ellul et al. (2003) find an increased order submission probability for all order types in volatile periods. According to Lo et al. (2002), limit orders execute more quickly when markets become more volatile (the authors use the logarithm of the number of trades in the previous hour as a proxy for volatility). Hasbrouck and Saar (2002) investigate the effects of volatility on the cross-section of companies traded on Island ECN. They find that increased volatility reduces the expected time to execution, which they label as a mechanistic volatility effect. These results are of paramount practical importance for the finance industry, since recent years have seen an unprecedented surge in automated trading. In sum, we think that far more attention should be paid to modeling intraday volatility, and we propose an important contribution to the existing literature.

The paper is organized as follows. Section 2 presents the model. Section 3 describes the data and gives results of estimation. This is followed by a forecasting section and conclusions.
2. THE MODEL

2.1. Notation

We use the following notation. Days in the sample are indexed by \( t \) (\( t = 1, \ldots, T \)). Each day is divided into 10 minute intervals referred to as bins and indexed by \( i \) (\( i = 0, \ldots, N \)). The current period is \( \{t,i\} \). The price of an asset at the end of bin \( i \) of day \( t \) is denoted by \( P_{\{t,i\}} \). The continuously compounded return \( r_{\{t,i\}} \) is modeled as:

\[
   r_{\{t,i\}} = \ln \left( \frac{P_{\{t+1,i\}}}{P_{\{t,i\}}} \right) \quad \text{for} \quad i \geq 1
\]

\[
   = \ln \left( \frac{P_{\{t+1\}}}{P_{\{t,N\}}} \right) \quad \text{for} \quad i = 0
\]

(1)

The overnight return in bin zero is deleted leading to a total number of return observations, \( M = TN \).

2.2. Model

We propose a new GARCH model for high frequency intraday financial returns, which specifies the conditional variance to be a multiplicative product of daily, diurnal and stochastic intraday volatility. Intraday equity returns are described by the following process:

\[
   r_{\{t,i\}} = \sqrt{h_i s_i q_{\{t,i\}}} \epsilon_{\{t,i\}} \quad \text{and} \quad \epsilon_{\{t,i\}} \sim N(0,1)
\]

(2)

where:

- \( h_i \) is the daily variance component,
- \( s_i \) is the diurnal (calendar) variance pattern,
- \( q_{\{t,i\}} \) is the intraday variance component with mean one, and
- \( \epsilon_{\{t,i\}} \) is an error term.

The daily variance component could be specified in a number of ways. Andersen and Bollerslev (1997, 1998), estimate this component from a daily GARCH model for a longer sample, going back a number of months or years. It could also be estimated based on daily realized variance as proposed by Engle and Gallo (2005). We adopt a different route, however, and utilize commercially available volatility forecasts produced daily for each company in our sample. This eliminates the need for longer series for the daily model than for the intra-daily
model. With the turnover of corporate ownership, it is difficult to get consistent long series for a big universe of stocks.

The diurnal component is calculated as the variance of returns in each bin after deflating by the daily volatility. To see this consider the variance of these returns:

\[ \frac{r_{i,j}^2}{h_j} = s_i q_{i,j} \epsilon_{i,j}^2 \]

and

\[ E \left( \frac{r_{i,j}^2}{h_j} \right) = s_i E \left( q_{i,j} \right) = s_i \]

(3)

Practically, we estimate the model in two stages. First we normalize returns by daily and diurnal volatility components, and then model the residual volatility as a unit GARCH(1,1) process:

\[ y_{i,t} = \frac{r_{i,t}}{\sqrt{h_t}} = \sqrt{q_{i,t} \epsilon_{i,t}^2} \]

(4)

\[ q_{i,t} = \omega + \alpha (r_{i,t-1} / \sqrt{\hat{h}_{i,t-1}})^2 + \beta q_{i,t-1} \]

(5)

The GARCH specification can be rewritten as:

\[ z_{i,t} \mid F_{i,t-1} \sim N \left( 0, q_{i,t} \right) \]

\[ q_{i,t} = \omega + \alpha z_{i,t-1}^2 + \beta q_{i,t-1} \]

(6)

The unit GARCH might enforce the constraint \( \omega = 1 - \alpha - \beta \) although in the empirical work this has not been done.

3. ECONOMETRIC ISSUES

In this section we will discuss statistical properties of the two-step estimator of the model outlined in the previous section. The estimation proceeds in two steps. First we specify and estimate the diurnal component. Following equation (3) we estimate the diurnal component for each bin as the variance of \( y_{i,t} \) in this bin. That is:

\[ \hat{s}_i = \frac{1}{T} \sum_{t=1}^{T} y_{i,t}^2, \quad \forall i = 1, ..., N \]

(7)

The second step consists of standardizing \( y_{i,t} \) by \( \sqrt{\hat{s}_i} \) and estimating parameters of the GARCH(p,q) model, which describes the dynamics of the intraday stochastic com-
ponent as in (6). Such a multi-step estimation strategy is potentially misleading as errors in one stage can lead to errors in the next stage. Nevertheless it will be shown below that the estimator is consistent but that the standard errors should be adjusted.

In deriving the asymptotic properties of the estimators in this sequential procedure, we will follow Newey and McFadden (1994) (later denoted as NM) and cast the above steps into the GMM framework. We will consider the GMM estimator of the moment conditions stacked one on the other. We will use the following notation. Vector \( \psi = \begin{pmatrix} \phi \\ \theta \end{pmatrix} \) contains both the \( k_1 \) parameters \( \phi \), estimated in the first step, and the \( k_2 \) parameters \( \theta \), estimated in the second step. Let there be \( k_1 \) moment conditions \( g_1(\phi) \) and \( k_2 \) moment conditions \( g_2(\phi, \theta) \) comprising vector \( g(\psi) = \begin{pmatrix} g_1(\phi) \\ g_2(\phi, \theta) \end{pmatrix} \). The corresponding sample sums are \( g_1M \) and \( g_2M \), giving \( g_M = (g_{1M}', g_{2M}')' \). We will consider the GMM estimator of the parameter vector

\[
\hat{\psi} = \begin{pmatrix} \hat{\phi} \\ \hat{\theta} \end{pmatrix} = \arg \min g_M 'Wg_M = \arg \min g_M 'g_M
\]

Since it is a just identified system, \( W=I \). To solve this system, \( \phi \) must solve the first set of equations and \( \theta \) must solve the second set conditional on the estimated value of \( \phi \). Thus it is a natural framework to analyze two step estimators of this type. Newey and McFadden (1994) (c.f. their Theorem 6.1, p. 2178), have shown that if \( \hat{\phi} \) and \( \hat{\theta} \) are consistent estimators of the true \( \phi_0 \) and \( \theta_0 \), respectively, and \( g_M \) satisfies a number of standard regularity conditions, the resulting GMM estimator is consistent and asymptotically normal:

\[
\sqrt{M} \begin{pmatrix} \hat{\phi} - \phi_0 \\ \hat{\theta} - \theta_0 \end{pmatrix} \overset{d}{\longrightarrow} N \left( 0, G^{-1} \Omega G^{-1} \right)
\]

where \( G = E \left( \frac{\partial g(\psi)}{\partial \psi} \right) \) and \( \Omega = E(g(\psi)g(\psi)) \).

As in Hansen (1982), the above matrices can be consistently estimated by replacing expectations by sample averages and parameters by their estimates.

The NM approach is very convenient and may be applied when parameters at some steps are estimated by ML. In this case some of the GMM moment conditions are taken
to be score functions. In the current two-step setting, the sample sums in the first and the second stages are:

\[
g_{1,M}(\phi) = g_{1,M} = \begin{pmatrix}
\frac{1}{T} \sum_{i=1}^{T} (y_{[t,i]}^2 - s_i) \\
\vdots \\
\frac{1}{T} \sum_{i=1}^{T} (y_{[t,N]}^2 - s_N)
\end{pmatrix}
\]  \hspace{1cm} (10)

\[
g_{2,M}(\phi, \theta) = g_{2,M} = 1/T \sum_{i=1}^{T} \sum_{j=1}^{N} \nabla_{\phi} \left( \log(q_{[t,i]}) + \left( y_{[t,j]}^2 / \hat{s}_{[t,j]} \right) \right)
\]  \hspace{1cm} (11)

\[
G = \frac{1}{M} \sum \begin{pmatrix}
\nabla_{\phi} g_1 \\
\nabla_{\phi} g_2
\end{pmatrix} \quad \text{and} \quad \frac{1}{M} \sum \begin{pmatrix}
g_{1,t} & g_{1,t} g_{2,t} \\
g_{1,t} g_{2,t} & g_{2,t}
\end{pmatrix} \xrightarrow{p} \Omega
\]  \hspace{1cm} (12)

In order to apply NM’s Theorem 6.1, we have to make sure that \( \hat{\phi} \) and \( \hat{\theta} \) are consistent estimators of the true parameter values at each stage. This is indeed the case for estimator (7). In random sampling from a stationary ergodic distribution, the sample mean is a consistent estimate of the expected value. Consistency of \( \hat{\theta} \) follows from, for example, Hansen and Lee (1994) or Lumsdaine (1996). In sum, the consistency and asymptotic normality of the estimator (11) is a corollary to Theorem 6.1 (p. 2178) in Newey and McFadden (1994). The above results could, in principle, be generalized to a multi-step estimation.

4. EMPIRICAL RESULTS

4.1. DATA

Our sample consists of price data on 2721 companies obtained from the TAQ database. We analyze logarithmic returns standardized by a commercially available volatility forecast for each company and each day and the standard deviation of returns in each 10-minute bin. The returns were calculated using transaction prices. The overnight return in bin zero has been deleted. Data spans a three-month period in April-June 2000.
4.2. RESULTS FOR A SINGLE STOCK

Some results will be presented using returns on a single randomly chosen NASDAQ-listed stock – Semitool Inc (SMTL). This company produces equipment for semiconductor industry. We divide 10-minute returns by their respective daily commercially available volatility forecasts. What can be observed for these data, however, is a very clear diurnal volatility pattern. Figure 1 plots the standard deviation of returns in each of 39 10-minute bins. There is a pronounced increased variation in the beginning of each day, a calmer period in the middle and somewhat increased variation towards the end. This diurnal pattern has been observed by many studies for all sorts of financial returns.

The sample variance for each bin will be our estimate of diurnal variance component $s_i$. Hence in the second step, returns are normalized by their respective diurnal standard deviations. In order to take account of the remaining intraday dynamics, we fit a GARCH (1,1) model into returns standardized in that way. Figure 2 superimposes the three volatility components described above. For clarity, we have chosen to show an approximately three-week period at the very beginning of the sample (3-25 April 2000). The bold blue line shows the daily volatility forecast, which is the same for all bins on a given day. The green thin line represents the regular diurnal pattern, and the stochastic intraday component appears in red with dotted marks. We may appreciate that this component is able to modify the regular deterministic diurnal pattern.

Figure 3 consists of five panels. Top panel shows logarithmic returns normalized by the unconditional standard deviation of the series. This is followed by the square roots of the estimated variance components: daily, diurnal and intraday. These are followed by the square root of a composite variance component, being the product of the preceding three variance components.
4.3. RESULTS FOR A SAMPLE OF 2721 STOCKS

4.3.1 SEPARATE ESTIMATION RESULTS

Model (6) is estimated for 2721 US stock equity returns, which have been previously divided by a volatility forecast for a day and “diurnally adjusted” by the standard deviation for each bin. Any remaining serial correlation is eliminated by fitting an ARMA(1,1). Estimation is performed for the period April-May 2000, and the combined count of observations during this period exceeds 4.2 million data points. Since it is rather demanding to fit results of estimation for 2721 separate companies into a table of a manageable size, we report results of this procedure resorting to graphical methods. Figure 4a shows parameter values for companies sorted by their trading intensity. By a “GARCH parameter” and an “ARCH parameter”, we refer to $\beta$ and $\alpha$ coefficients from equation (5). The top and middle panels of Figure 4a depict $\beta$ and $\alpha$ parameters, respectively. The bottom panel plots the sum of both parameters, thus informing us how persistent the volatility is. Figure 4b offers a histogram of this measure of persistence ($\beta + \alpha$). In both figures, we may observe a fair amount of variation in the values of parameters and the measure of persistence. For the purpose of this graphical illustration, the companies are sorted according to their trading intensity. Here we measure trading intensity by the average daily number of trades.

Companies at the left of Figure 4a are very actively traded, and at the very right—trade seldom. It can be observed that estimates’ variability decreases with the trading intensity. Further, there is an upward trend in the GARCH parameter and a downward tendency for the ARCH parameter. In fact, Figures 4a and 4b give us a rationale for grouping companies for the purpose of estimation. It turns out that for some companies, especially the least trading ones, separate GARCH estimation encounters difficulties, predominantly of a numerical nature. When we inspected the “troubled” companies more closely, estimation problems were usually resolved by removing, one or two very influential observations (of a magnitude of 10 standard deviations or so). This however seems to be a rather arbitrary procedure. When confronted with a big cross section of companies, as in this paper, such arbitrary practice could prove very tedious and virtually impossible in real-time big scale implementation.
4.3.2 GROUPED ESTIMATION RESULTS

As discussed in previous section, Figure 4a indicates that for some companies, particularly the less liquid ones, mainly due to the widespread presence of influential or outlying observations, numerical problems with convergence are more likely. We seek to use the cross-section information, to improve estimation results. We will judge the performance of particular models on the basis of their forecasting results, presented in sections following the present one.

The purpose is to group/pool companies and estimate a GARCH model for each group. Just as in the case of pooled OLS estimation, we append one series to the end of the previous one. However, we must normalize each company returns by its standard deviation to prevent the switching point from being a structural break.

An important question we need to answer is what a good criterion for grouping should be. Grouping similar companies increases the sample size and will improve accuracy. However grouping dissimilar companies will introduce bias. The way we group series could certainly influence the parameters of model (6). Although industry grouping is an obvious candidate, we have investigated a number of different admissible ways of sorting companies.

We have attempted to classify groups based on the exchange the stocks are traded on and if they are included in major indices. In particular we have obtained 5 groups: NYSE/NASDAQ exchange and S&P and non-S&P equities, with the remaining 5th category “Other stocks”. This exercise was motivated by the finding reported by some authors (c.f. Bennett and Wei, 2003) documenting changing volatility levels for companies that have switched exchanges. Our five groups turned out to be very unbalanced in terms of size, and the forecast comparison seemed to be worse than the other grouping modes applied. Therefore we do not report results of this exercise in this paper.

Another approach to pooling stocks is to sort them by time series characteristics. As previously mentioned, Figure 4a suggests a liquidity criterion for pooling companies into groups. We have tried several categories: we have grouped companies according to their capitalization and intensity of trading measured as both the average number of trades per day and the percentage of zero returns. Capitalization grouping placed companies with visibly different volatility patterns into the same groups and it underperformed other measures in forecasting. In the rest of the paper, our favorite liquidity criterion will be the average number of trades per day. However, estimation and forecasting results were indistinguishable for the percentage of zero returns as a criterion for sorting.
In summary, we will investigate three different ways of sorting companies into groups. INDUST denotes a GARCH estimation for companies grouped according to their primary industry classification. In LIQUID mode we have grouped companies according to the average number of trades per day. The last mode (ONEBIG) involves estimation of a single large GARCH model, for all companies pooled together into one group.

[INSERT TABLES 2-4 AND FIGURES 5-7 ABOUT HERE]

In the INDUST mode we group data into 54 industries and estimate 54, instead of 2721 intraday GARCH (1,1) models. Each return series has been divided by its standard deviation in order to render returns comparable across stocks. Estimation results of this step are summarized in Table 2 and parameters plotted in Figure 5. We do not encounter any convergence problems as was the case for some companies in individual estimation. The persistence parameter for most industries falls in the range of 0.86-0.96, and the minimum value is 0.761. Please note that the persistence values are lower than it is customary for daily GARCH models. This however does not contradict temporal aggregation results of Drost and Nijman (1993), since we have previously removed the daily volatility component, responsible for a longer persistence.

Next we estimate GARCH models for 50 groups of companies sorted according to the liquidity criterion. Table 3 gives results and Figure 6 plots parameters. A somewhat disappointing result emerging from Table 3 is that most of the actively traded groups produce GARCH residuals that show statistically significant volatility clustering (as indicated by ARCH LM(1) and LM(20) tests). It appears, however, that this sorting mode works well for less liquid stocks, a finding that will be reinforced by forecasting comparisons. Histogram in Figure 6b seemingly documents a reduction in intraday GARCH parameter variation with one notable exception. The least liquid group comprising 55 companies has a persistence parameter equal to 0.575. This group is characterized by spectacular kurtosis and skewness coefficients. Figure 7 gives a snapshot of 10-minute returns on the least trading stocks and modestly trading stocks. The bulk of observations in least trading group are equal to zero, and many nonzero observations could be described as outlying or “influential” because they equal to several standard deviations from the mean.

Finally, Table 4 reports results for ARCH estimation for the intraday component for one giant pool of all the companies, comprising over 4.2 million observations. Similar to the industry case, this table also indicates modest persistence of intraday volatility.
5. FORECASTING RESULTS

5.1. LOSS FUNCTIONS AND DESIGN

We now turn to out of sample forecast accuracy. We use the parameter estimates for the period April-May 2000, and forecast one-step-ahead volatilities for each bin in June 2000. Forecasts are obtained in a sequential procedure on the basis of estimated parameters and the volatility forecast calculated at previous bin, as well as actual returns from the previous bin. From the structure of the model, forecasts of the variance of returns are the product of the daily variance forecast, the diurnal variance and the GARCH variance. In this analysis, the variance that is forecast is of the return deflated by the daily volatility times the diurnal volatility. In the forecast period the daily volatility is taken from the same commercial source as for the estimation period.

It should be appreciated that forecasting volatility is connected with an additional complication since of course we do not observe the variable we want to forecast. In our forecasting evaluation we will compare our forecasts with the squared return \( z_{t,t}^2 = r_{t,t}^2 / \hat{h}_t \delta_t \). This return is a random variable drawn from a distribution with a variance we are trying to estimate. We expect that the squared return will be large only when the true variance is large, however, the squared return may be small even when the variance is large. As a consequence, it is not at all clear what a sensible loss function should be. For recent discussions of forecast accuracy measures, see Granger (2003) or Patton (2004). In the following, we use two loss functions:

\[
L_1 = \log q_{t,t} + \frac{z^2_{t,t}}{q_{t,t}}
\]

\[
L_2 = (z^2_{t,t} - q_{t,t})^2
\]

The use of squared return in place of the true volatility introduces biases in many popular loss functions problematic (so does the RV measure, c.f. Patton, 2004). However, under MSE and LIK loss functions optimal forecasts are unbiased (c.f. Patton, 2004 and Hansen and Lunde, 2005).

Although part of the literature on assessing forecasting performance of daily models (c.f. Hansen and Lunde, 2004) recommends using RV as a proxy, this paper uses squared returns because 10 minute interval does not allow a reliable measure of realized volatility to be estimated. For many of the companies in our sample and outside of the
active trading periods, the small numbers of trades in 10-minute bins raised concern about the precision of RV estimates.

We determine forecasts for each company separately, using parameters estimated in both separate and pooled estimations. Therefore for each time period, for each company, we obtain 5 different forecasts that will form the basis for a subsequent model evaluation and comparison.

5.2. OUT-OF-SAMPLE FORECAST COMPARISON

We have performed five different estimations for companies pooled into groups in various ways and will refer to these ways as modes. The first mode (NSTOCH) contains no stochastic component (5) at all. Mode No. 2 (UNIQUE) involves no pooling, i.e. we estimate unique GARCH models for separate companies. Mode No. 3 (INDUST) denotes a GARCH estimation for companies grouped according to their primary industry classification. In Mode No. 4 (LIQUID) we have grouped companies according to the average number of trades per day. The last mode (ONEBIG) involves estimation of a large GARCH model, for all companies pooled together to form one group.

For each of these 5 separate estimations we have calculated a series of forecast errors. These forecast errors are used to calculate accuracy measurement criteria using loss functions $L_1$ and $L_2$, $L_j = \frac{1}{\tau} \sum_{t=1}^{\tau} L_{jt}$, where $j=1,2$; $\tau=858$ and $\tau$ denotes the length of the forecasting period.

Table 5 compares accuracy of volatility forecasts obtained from the above estimation modes. We have calculated two forecast accuracy measures for each of the 5 estimations and for each company, which amounts to a total of (5 modes*2 criteria * 2721 stocks =) 27210 numbers. Then for each company we have compared performance of different modes of estimation pair by pair, and calculated a percentage of times a forecast from a given estimation outperforms each of the remaining forecasts. Hence, numbers contained in Table 5 give us the frequency with which the mode in the row outperforms the mode in the column for a particular loss function. We will first focus our attention on the upper panel of Table 5, which presents results of forecast comparison using LIK loss function. For example, the third row second column compares results of NSTOCH vs. separate GARCH estimations. Here the number 0.618 means that the specification without component (5) yields worse forecasts than the individual company-by-company estimation 62% of times. The second column of the table informs us that NSTOCH estimation performs worse than all the other modes.
As we learn from column three, separate estimation gives worse forecasting results than INDUST, LIQUID and ONEBIG modes, but outperforms NSTOCH. The fifth column establishes forecasting inferiority of LIQUID mode in comparison to both INDUST and ONEBIG modes. Finally the sixth column offers ONEBIG mode as a winner of this competition. The above discussion carries over to the lower panel of Table 5, which presents results for L1K loss function. One exception is that the MSE criterion marginally favours INDUST estimation over ONEBIG model. Taking into account the criticism directed at the MSE loss function as being unduly influenced by a few big errors, we think that overall ONEBIG mode emerges as a winner of the forecasting comparison.

Table 6 pertains to the same set of forecasting results as Table 5. It reports the mean and median of the forecast accuracy measures calculated for each of the 2721 companies and five estimation modes. The smallest number in each row denotes the smallest mean or median error. This table also contains the ordering that L1K and MSE criteria assign to the five estimation modes. Rank 1 denotes the best model, with the smallest error, model numbered as fifth performs the worst. Starting from the top panel, the liquidity sorted model appears to give the smallest mean errors for both loss functions. Please note that UNIQUE GARCH outperforms the model with no stochastic intraday component. We test the differences in the value of mean estimates of forecast errors using the Diebold Mariano (1995) tests reported in Table 7. This table presents t-values for the null hypothesis that the difference in forecast errors is zero. Note that if the model in the row forecasts worse than the model in the column, the t-ratio is negative. Column (or Row) 5 indicate that, according to the L1K loss function, liquidity sorting gives significantly better mean forecasts than the other models.

The lower panel of Table 6 contains medians of the forecast accuracy measures. Here ONEBIG model performs best, similarly to what we have concluded from Table 5.

Tables 5 and 6 give somewhat conflicting answers to the question - which method of company grouping should be adopted. However they agree that grouping is very desirable compared with separate estimation. We investigate the supposed disagreement looking at liquidity issues. We limit our attention to two separate samples of 550 most liquid and most illiquid companies. Table 8.A reports forecast accuracy measures for the subsample of least liquid stocks. Please note that means of error functions are bigger for least liquid stocks than for most liquid stocks (Table 8.B.). Nowhere is the difference between both tails so visible as for the MSE measure. The numbers differ by an order of a magnitude, and this illustrates the sensitivity of the MSE criterion to outlying observations, more frequently haunting illiquid stocks. Similar to conclusions from
Table 6, Table 8.A recommends liquidity sorted GARCH model as a preferred forecasting tool for illiquid stocks.

[INSERT TABLE 8 ABOUT HERE]

The picture suddenly changes when we look at the results assembled in Table 8.B, which concern the most liquid stocks. Here ONEBIG GARCH solution, followed closely by industry grouping outperform both liquidity-sorted models and separate estimation. These conclusions closely resemble results reported in Table 5.

To sum up, we have seen that inclusion of stochastic intraday component (5) improves forecasting results in comparison with the model with diurnal and daily components only. We also observe better forecasting performance using cross section information, and applying different methods of pooling. The exact way we chose to group companies heavily relies on company characteristics, liquidity in this case. Most liquid stocks seem to benefit from the widest pooling possible, i.e. using all available cross section information. Most illiquid stocks apparently exhibit intraday dynamics which are idiosyncratic to their particular liquidity-determined group, and consequently we may obtain better forecasts when we group these stocks together.

6. CONCLUSION

This paper proposes a new way of modeling and forecasting intraday returns. We decompose the volatility of high frequency asset returns into components that may be easily interpreted and estimated. The conditional variance is expressed as a product of daily, diurnal and stochastic intraday volatility components. This model is applied to a comprehensive sample consisting of 10-minute returns on more than 2500 US equities.
REFERENCES


Engle, R. F. (2005), Integrating Investment Risk and Trading Risk, manuscript, Department of Finance, NYU.


### Table 1. SMTL Intraday GARCH Results

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Standard Error</th>
<th>T Statistic</th>
</tr>
</thead>
<tbody>
<tr>
<td>C</td>
<td>0.0013</td>
<td>0.0177</td>
<td>0.0726</td>
</tr>
<tr>
<td>ω</td>
<td>0.1896</td>
<td>0.0208</td>
<td>9.1076</td>
</tr>
<tr>
<td>β</td>
<td>0.6814</td>
<td>0.0293</td>
<td>23.2738</td>
</tr>
<tr>
<td>α</td>
<td>0.1295</td>
<td>0.0130</td>
<td>9.9463</td>
</tr>
</tbody>
</table>

**Notes:** This table presents estimation results for intraday GARCH(1,1) model for Semitools Inc. Sample period April-May 2000. Symbols α, β and ω denote GARCH parameters from the variance equation (5). C denotes a constant in the mean equation.
Table 2. Industry Sorting Estimation Results - INDUST Mode

<table>
<thead>
<tr>
<th>Industry</th>
<th>Skewness coefficient</th>
<th>Kurtosis coefficient</th>
<th>No. of observations</th>
<th>αβ</th>
<th>α</th>
<th>t-stat</th>
<th>β</th>
<th>t-stat</th>
<th>α</th>
<th>t-stat</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>-0.17</td>
<td>19.6</td>
<td>92907</td>
<td>0.13</td>
<td>0.1</td>
<td>0.065</td>
<td>105.2</td>
<td>-258309.7</td>
<td>0.065</td>
<td>-258338.1</td>
</tr>
<tr>
<td>2</td>
<td>0.09</td>
<td>21.6</td>
<td>24100</td>
<td>0.24</td>
<td>0.0</td>
<td>0.065</td>
<td>105.2</td>
<td>-258309.7</td>
<td>0.065</td>
<td>-258338.1</td>
</tr>
<tr>
<td>3</td>
<td>-0.33</td>
<td>22.7</td>
<td>71292</td>
<td>0.14</td>
<td>0.1</td>
<td>0.065</td>
<td>105.2</td>
<td>-258309.7</td>
<td>0.065</td>
<td>-258338.1</td>
</tr>
<tr>
<td>4</td>
<td>0.12</td>
<td>18.4</td>
<td>134191</td>
<td>0.13</td>
<td>0.1</td>
<td>0.065</td>
<td>105.2</td>
<td>-258309.7</td>
<td>0.065</td>
<td>-258338.1</td>
</tr>
<tr>
<td>5</td>
<td>0.15</td>
<td>14.9</td>
<td>100759</td>
<td>0.06</td>
<td>0.1</td>
<td>0.065</td>
<td>105.2</td>
<td>-258309.7</td>
<td>0.065</td>
<td>-258338.1</td>
</tr>
<tr>
<td>6</td>
<td>-0.01</td>
<td>11.9</td>
<td>43464</td>
<td>0.09</td>
<td>0.5</td>
<td>0.065</td>
<td>105.2</td>
<td>-258309.7</td>
<td>0.065</td>
<td>-258338.1</td>
</tr>
<tr>
<td>7</td>
<td>-0.22</td>
<td>12.9</td>
<td>55380</td>
<td>0.11</td>
<td>0.0</td>
<td>0.065</td>
<td>105.2</td>
<td>-258309.7</td>
<td>0.065</td>
<td>-258338.1</td>
</tr>
<tr>
<td>8</td>
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<td>16.8</td>
<td>102688</td>
<td>0.15</td>
<td>0.0</td>
<td>0.065</td>
<td>105.2</td>
<td>-258309.7</td>
<td>0.065</td>
<td>-258338.1</td>
</tr>
<tr>
<td>9</td>
<td>-0.04</td>
<td>30.3</td>
<td>23671</td>
<td>0.11</td>
<td>0.0</td>
<td>0.065</td>
<td>105.2</td>
<td>-258309.7</td>
<td>0.065</td>
<td>-258338.1</td>
</tr>
<tr>
<td>10</td>
<td>0.61</td>
<td>21.6</td>
<td>10647</td>
<td>0.18</td>
<td>0.0</td>
<td>0.065</td>
<td>105.2</td>
<td>-258309.7</td>
<td>0.065</td>
<td>-258338.1</td>
</tr>
<tr>
<td>11</td>
<td>-0.09</td>
<td>16.2</td>
<td>37322</td>
<td>0.16</td>
<td>0.0</td>
<td>0.065</td>
<td>105.2</td>
<td>-258309.7</td>
<td>0.065</td>
<td>-258338.1</td>
</tr>
<tr>
<td>12</td>
<td>-0.38</td>
<td>32.0</td>
<td>28236</td>
<td>0.23</td>
<td>0.0</td>
<td>0.065</td>
<td>105.2</td>
<td>-258309.7</td>
<td>0.065</td>
<td>-258338.1</td>
</tr>
<tr>
<td>13</td>
<td>0.19</td>
<td>19.4</td>
<td>33540</td>
<td>0.18</td>
<td>0.2</td>
<td>0.065</td>
<td>105.2</td>
<td>-258309.7</td>
<td>0.065</td>
<td>-258338.1</td>
</tr>
</tbody>
</table>

**Notes:** This table presents estimation results for intraday GARCH(1,1) models for 54 industries. Sample period April-May 2000. Symbols α, β, and ω denote GARCH parameters from the variance equation (5). Persistence is measured as the sum of parameters (α + β). AIC and BIC denote Akaike and Schwartz Information Criteria, respectively. LM(1) and LM(20) statistics are calculated as the ARCH LM test, cf. Engle (1982), under the null of no ARCH effects at lag q. ** indicates significance at the 5% and 1% levels, respectively.
the ARCH LM test, cf. Engle (1982), on the residuals from (6). Under the null of no ARCH effects at lag

\[ \alpha \] and \[ \beta \] denote Akaike and Schwarz Information Criteria, respectively. LM(1) and LM(20) statistics are calculated as

\[ \beta - \alpha \] from the variance equation (5). Persistence is measured as the sum of parameters (\[ \alpha + \beta \]) at 1% levels, respectively.

Sample period April-May 2000. Symbols * denote significance at the 5% level, ** at 1% levels.

Notes: This table presents estimation results for intraday GARCH(1,1) models for 50 groups of liquidity sorted companies. Sample period April-May 2000. Symbols \( \alpha \), \( \beta \) and \( \omega \) denote GARCH parameters from the variance equation (5). Persistence is measured as the sum of parameters (\( \alpha + \beta \)). AIC and BIC denote Akaike and Schwartz Information Criteria, respectively. LM(1) and LM(20) statistics are calculated as the ARCH LM test, cf. Engle (1982), on the residuals from (6). Under the null of no ARCH effects at lag \( q \), the statistic has a chi2 distribution with \( q \) degrees of freedom, where \( q = 1, 20 \). * , ** denote significance at the 5% and 1% levels, respectively.
Table 4. All Sample Estimation Results- ONEBIG Mode

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Standard Error</th>
<th>T Statistic</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\omega$</td>
<td>0.096</td>
<td>0.000112</td>
<td>854.3</td>
</tr>
<tr>
<td>$\beta$</td>
<td>0.823</td>
<td>0.000180</td>
<td>4570.4</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>0.084</td>
<td>0.000115</td>
<td>728.6</td>
</tr>
</tbody>
</table>

Notes: This table presents estimation results for intraday GARCH(1,1) models for one large group of companies pooled together. Sample period April-May 2000. Symbols $\alpha$, $\beta$ and $\omega$ denote GARCH parameters from the variance equation (5).

Table 5. Comparison of one-period-ahead forecasts for estimation modes
Frequency with which the mode in a row outperforms the mode in a column

<table>
<thead>
<tr>
<th>Modes</th>
<th>NSTOCH</th>
<th>UNIQUE</th>
<th>INDUST</th>
<th>LIQUID</th>
<th>ONEBIG</th>
</tr>
</thead>
<tbody>
<tr>
<td>NSTOCH</td>
<td>0.382</td>
<td>0.275</td>
<td>0.245</td>
<td>0.262</td>
<td></td>
</tr>
<tr>
<td>UNIQUE</td>
<td>0.618</td>
<td>0.354</td>
<td>0.404</td>
<td>0.339</td>
<td></td>
</tr>
<tr>
<td>INDUST</td>
<td>0.725</td>
<td>0.646</td>
<td>0.572</td>
<td>0.445</td>
<td></td>
</tr>
<tr>
<td>LIQUID</td>
<td>0.755</td>
<td>0.596</td>
<td>0.428</td>
<td>0.377</td>
<td></td>
</tr>
<tr>
<td>ONEBIG</td>
<td>0.738</td>
<td>0.661</td>
<td>0.555</td>
<td>0.623</td>
<td></td>
</tr>
</tbody>
</table>

Notes: This table compares accuracy of one-step-ahead volatility forecasts obtained from five estimation modes. It contains frequency with which a forecast from an estimation described in a row outperforms a forecast from an estimation mode indicated in the column. Top panel: forecasts comparisons using LIK (Out-of-sample likelihood) loss function. Second panel: Forecasts comparison using MSE loss function.
Table 6. Mean and median of forecast accuracy measures for individual stocks

<table>
<thead>
<tr>
<th>Loss function</th>
<th>NSTOCH</th>
<th>UNIQUE</th>
<th>INDUST</th>
<th>LIQUID</th>
<th>ONEBIG</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Mean of forecasts accuracy measures</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>LIK</td>
<td>Mean</td>
<td>1.0001</td>
<td>0.9485</td>
<td>0.9306</td>
<td>0.9271</td>
</tr>
<tr>
<td></td>
<td>Rank</td>
<td>5</td>
<td>4</td>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>MSE</td>
<td>Mean</td>
<td>3.4930</td>
<td>3.4835</td>
<td>3.4668</td>
<td>3.4661</td>
</tr>
<tr>
<td></td>
<td>Rank</td>
<td>5</td>
<td>4</td>
<td>3</td>
<td>1</td>
</tr>
<tr>
<td><strong>Median of forecasts accuracy measures</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>LIK</td>
<td>Median</td>
<td>1.0002</td>
<td>0.9543</td>
<td>0.9430</td>
<td>0.9432</td>
</tr>
<tr>
<td></td>
<td>Rank</td>
<td>5</td>
<td>4</td>
<td>2</td>
<td>3</td>
</tr>
<tr>
<td>MSE</td>
<td>Median</td>
<td>2.9765</td>
<td>2.9571</td>
<td>2.9495</td>
<td>2.9498</td>
</tr>
<tr>
<td></td>
<td>Rank</td>
<td>5</td>
<td>4</td>
<td>2</td>
<td>3</td>
</tr>
</tbody>
</table>

*Top panel contains sample means of the forecast accuracy measures calculated for five estimation modes for each company separately for both loss functions. Second panel contains sample medians of the forecast accuracy measures.*

*Rows labeled “Rank” indicates the ranking of models on the basis of their mean (or median) errors. Models with smallest errors are ranked as 1, the worst models are assigned the rank number 5.*
Table 7. Forecast accuracy Diebold-Mariano test, t-values

<table>
<thead>
<tr>
<th>Modes</th>
<th>NSTOCH</th>
<th>UNIQUE</th>
<th>INDUST</th>
<th>LIQUID</th>
<th>ONEBIG</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>LIK loss function</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>NSTOCH</td>
<td>-5.8297 *</td>
<td>-35.772 *</td>
<td>-40.947 *</td>
<td>-34.688 *</td>
<td></td>
</tr>
<tr>
<td>UNIQUE</td>
<td>5.8297 *</td>
<td>-2.074 *</td>
<td>-2.459 *</td>
<td>-1.998 *</td>
<td></td>
</tr>
<tr>
<td>INDUST</td>
<td>35.772 *</td>
<td>2.074 *</td>
<td>-4.964 *</td>
<td>1.367</td>
<td></td>
</tr>
<tr>
<td>LIQUID</td>
<td>40.947 *</td>
<td>2.459 *</td>
<td>4.964 *</td>
<td>5.351 *</td>
<td></td>
</tr>
<tr>
<td>ONEBIG</td>
<td>34.688 *</td>
<td>1.998 *</td>
<td>-1.367</td>
<td>-5.351 *</td>
<td></td>
</tr>
<tr>
<td><strong>MSE loss function</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>NSTOCH</td>
<td>-3.5983 *</td>
<td>-22.176 *</td>
<td>-23.956 *</td>
<td>-20.394 *</td>
<td></td>
</tr>
<tr>
<td>UNIQUE</td>
<td>3.598 *</td>
<td>*</td>
<td>-7.404 *</td>
<td>-7.481 *</td>
<td>-7.322 *</td>
</tr>
<tr>
<td>INDUST</td>
<td>22.176 *</td>
<td>7.404 *</td>
<td>-1.377</td>
<td>-0.335</td>
<td></td>
</tr>
<tr>
<td>LIQUID</td>
<td>23.956 *</td>
<td>7.481 *</td>
<td>1.377</td>
<td>-0.624</td>
<td></td>
</tr>
<tr>
<td>ONEBIG</td>
<td>20.394 *</td>
<td>7.322 *</td>
<td>0.334</td>
<td>-0.624</td>
<td></td>
</tr>
</tbody>
</table>

Notes: This table presents t-values for the null hypothesis that the difference in forecast errors between estimation modes is not significantly different from zero. If the model in the row forecasts worse than the model in the column, the t-ratio is negative. * denotes significance at the 5% level.
Table 8. Forecast accuracy comparison for most and least liquid stocks

### A. Least Liquid Stocks

<table>
<thead>
<tr>
<th>Forecast accuracy measures</th>
<th>LIK</th>
<th>Rank</th>
<th>MSE</th>
<th>Rank</th>
<th>Av. Rank</th>
</tr>
</thead>
<tbody>
<tr>
<td>NSTOCH No stochastic intraday component</td>
<td>1.0002</td>
<td>5</td>
<td>5.8425</td>
<td>2</td>
<td>3.5</td>
</tr>
<tr>
<td>UNIQUE Separate GARCH estimation</td>
<td>0.9779</td>
<td>4</td>
<td>5.8871</td>
<td>5</td>
<td>4.5</td>
</tr>
<tr>
<td>INDUST Industry GARCH estimation</td>
<td>0.9548</td>
<td>2</td>
<td>5.8481</td>
<td>3</td>
<td>2.5</td>
</tr>
<tr>
<td>LIQUID Liquidity-Sorted GARCH estimation</td>
<td>0.9405</td>
<td>1</td>
<td>5.8287</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>ONEBIG One large GARCH estimation</td>
<td>0.9629</td>
<td>3</td>
<td>5.8541</td>
<td>4</td>
<td>3.5</td>
</tr>
</tbody>
</table>

### B. Most Liquid Stocks

<table>
<thead>
<tr>
<th>Forecast accuracy measures</th>
<th>LIK</th>
<th>Rank</th>
<th>MSE</th>
<th>Rank</th>
<th>Av. Rank</th>
</tr>
</thead>
<tbody>
<tr>
<td>NSTOCH No stochastic intraday component</td>
<td>0.9999</td>
<td>5</td>
<td>2.7439</td>
<td>5</td>
<td>5</td>
</tr>
<tr>
<td>UNIQUE Separate GARCH estimation</td>
<td>0.9679</td>
<td>4</td>
<td>2.7309</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>INDUST Industry GARCH estimation</td>
<td>0.9293</td>
<td>2</td>
<td>2.7084</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>LIQUID Liquidity-Sorted GARCH estimation</td>
<td>0.9339</td>
<td>3</td>
<td>2.7172</td>
<td>3</td>
<td>3</td>
</tr>
<tr>
<td>ONEBIG One large GARCH estimation</td>
<td>0.9274</td>
<td>1</td>
<td>2.7044</td>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>

Notes: This table reports forecast accuracy measures for the subsample of least liquid stocks (top panel) and most liquid stocks (second panel). Rank denotes ordering from best (1) to worst (4). Average Rank is calculated as the mean of ordering measures in each row. LIK and MSE are two loss functions used.
Figure 1. Standard deviation of returns across bins for SMTL stock. The horizontal axis labels denote hours during a trading day. Values depicted in this graph are calculated as a standard deviation of 10-min returns in each bin. Returns have been previously divided by daily volatility components.

Figure 2. Volatility Components for Semitools Inc. This figure superimposes square roots of variance components estimated for SMTL, Semitools Inc. For clarity this picture offers a snapshot for the period 3-25 April 2000. The bold line shows the daily volatility forecast, which is the same for all bins on a given day. The green thin line represents the regular diurnal pattern, and the stochastic intraday component appears in red with dotted marks.
Figure 3. Volatility Components for Semitools Inc. Estimation period April-May 2000.  
Top panel: Logarithmic intraday returns on SMTL stock normalized by their unconditional standard deviation.  
Second panel: The square root of the daily variance component.  
Third panel: The square root of the diurnal variance component.  
Fourth panel: The square root of the intraday variance component.  
Fifth panel: The square root of the composite variance component being the product of the proceeding three variance components.
Figure 4a. Estimation results for the intraday GARCH models for 2721 separate companies. Sample period April-May 2000. For the purpose of this picture companies were sorted by their average daily number of trades. *Top panel:* GARCH $\beta$ from equation (5). *Second panel:* ARCH parameter $\alpha$ from equation (5). *Third panel:* Persistence measure ($\alpha + \beta$).

Figure 4b. Histogram of the persistence measure ($\alpha + \beta$) from intraday GARCH estimation for 2721 Separate Models. Sample period April-May 2000. The horizontal axis denotes the value of the persistence parameter ($\alpha + \beta$) and the vertical axis denotes the number of companies with the estimated persistence parameters falling into a corresponding bin.
Figure 5a. Estimation results for the intraday GARCH models for 54 industries. Sample period April-May 2000. First panel: GARCH parameter $\beta$ from equation (5). Second panel: ARCH parameter $\alpha$ from equation (5). Third panel: Persistence measure ($\alpha + \beta$).

Figure 5b. Histogram of the persistence measure ($\alpha + \beta$) from intraday GARCH estimation for 54 industries. Sample period April-May 2000. The horizontal axis denotes the value of the persistence parameter ($\alpha + \beta$) and the vertical axis denotes the number of companies with the estimated persistence parameters falling into a corresponding bin.
Figure 6a. Estimation results for the intraday GARCH models for 50 liquidity-sorted groups. Trading intensity or liquidity increases from the left to the right side of each picture. Sample period April-May 2000. First panel: GARCH parameter $\beta$ from equation (5). Second panel: ARCH parameter $\alpha$ from equation (5). Third panel: Persistence measure ($\alpha+\beta$).

Figure 6b. Histogram of the persistence measure ($\alpha+\beta$) from intraday GARCH estimation for 50 liquidity-sorted groups. Sample period April-May 2000. The horizontal axis denotes the value of the persistence parameter ($\alpha+\beta$) and the vertical axis denotes the number of companies with the estimated persistence parameters falling into a corresponding bin.
A. Least Trading Group (1/50)

B. Modestly Trading Group (15/50)

Figure 7. Examples of standardized logarithmic returns for two of the 50 Liquidity-Sorted Groups. Horizontal axis denotes $i$th observation in each liquidity sorted group and snapshots were chosen at random from the upper half of the groups.